

# MATH FLUENCY FRAMEWORK

## ESSENTIAL ELEMENTS

1

### Understand

#### Research Framework

- 4 Elements of Fluency
- Cycle of Engagement
- Automaticity
- Practice
- Math Talk
- Modeling Mathematical Thinking
- Students Engagement

#### Shared Definitions

- School Administrators
- Teachers
- Students
- Parents

2

### Assess

#### Get the Data (build fluency profile)

- Do you check to see if the students come into the grade at the beginning of the year with at the fluency level from the grade before?
- Do you focus on fluency for 10 minutes a day, collecting evidence of practice sometimes?
- Do you assess fluency at the beginning, middle and end of the year?
- Is fluency more than a unit of study?
- Is fluency practice differentiated for students depending on where they are on the trajectory?
- Other

#### Use the Data

- Make an Individual Fluency Plan
- Student Goal Setting
- Make Acceleration Plans
- Map out Daily Fluency Routines

3

### Prepare

#### Classroom Design

- Differentiated Fluency Workstations
- Fluency Anchor Charts (Class Strategy Models Learning Target/ Success Criteria)
- Classroom Library (section on fluency books)

#### Materials

- Fact Fluency Folders
- Fact Fluency Rings
- Fluency Progressions
- Strategy Anchor Charts
- Model Anchor Charts
- Goal Setting
- Progress Monitoring
- Certificates
- Fact Fluency Parent Brochures/Newsletters by Grade
- Fact Fluency Videos by Operation
- Fact Fluency Website
- Student-created strategy cards
- Core set of manipulatives/ tools (domino, dice, 2 sided counters, cubes, highlighters, colored pencils, different types of paper (grid, centimeter, blank), rulers, number paths, beaded number lines, number lines and hundred grids).
- Plan Family Math Fluency Days & Nights

4

### Teach

#### Instruction

- Daily Routines- Whole Group
- Workstations - Individual, Partners, Small Group
- Guided Math Groups
- Personalized Goal Setting
- Homework

#### Assessment (Ongoing)

- Math Running Records
- Entrance/Exit Slips
- Observations
- Anecdotal
- Interviews
- Conferring
- Student Reflection
- Teacher Made Tests
- Standardized Tests

5

### Reflect/Revise

#### Analyze the Data (weekly, monthly, quarterly)

- Individually
- Class
- Grade
- Grade Band
- School

#### Interpret the Trends and Adjust Instruction Accordingly

- Individually
- Class

# Understand

## 1 Research Framework

- 4 Elements of Fluency
- Cycle of Engagement
- Automaticity
- Practice
- Math Talk
- Modeling Mathematical Thinking
- Students Engagement

## 2 Shared Definitions

- Teachers
- Students
- Parents

# Assess (Current State of Affairs)

## 3 Get the Data - (build fluency profile)

- Do you check to see if the students come into the grade at the beginning of the year with at the fluency level from the grade before?
- Do you focus on fluency for 10 minutes a day, collecting evidence of practice sometimes?
- Do you assess fluency at the beginning, middle and end of the year?
- Is fluency more than a unit of study?
- Is fluency practice differentiated for students depending on where they are on the trajectory

## 4 Use the Data

- Make an Individual Fluency Plan
- Student Goal setting
- Make Acceleration Plans
- Map out Daily Fluency Routines

# Prepare

## 5 Classroom Design

- Differentiated Fluency Workstations
- Fluency Anchor Charts (Class)
  - Strategy
  - Models
  - Learning Target/Success Criteria
- Classroom library (section on fluency books)

## 6 Materials

- Fact Fluency Folders (Progression, Goal Setting, Progress monitoring, certificates, anchor charts (individual), fluency rings)
- Fact Fluency Parent Brochures/Newsletters by Grade
- Fact Fluency Videos by Operation
- Fact Fluency Website
- Student-created strategy cards
- Core set of manipulatives (domino, dice, 2 sided counters, unifix cubes or snap cubes, highlighter, colored pencils, different types of paper (grid, centimeter, blank), rulers, cuisenaire rods, beaded number lines,

# Teach

## 7 Instruction

- Daily Routines- Whole Group
- Workstations - Individual, Partner, Small
- Guided Math Groups
- Personalized Goal Setting
- Homework

## 8 Assessment (Ongoing)

- Math Running Records
- Entrance/Exit Slips
- Observations
- Anecdotal
- Interviews
- Conferring
- Student Reflections
- Teacher Made Tests
- Standardized Tests
- Other

# Reflect/Revise

## 9 Analyze the Data (weekly, monthly, quarterly)

- Individually
- Class
- Grade
- Grade Band
- School

## 10 Interpret the Trends and Adjust Instruction Accordingly

- Individually
- Class

# 1

# Research Framework

Beginning

Approaching

Meeting

Exceeding

## 1.1 4 Elements of Fluency

- Accuracy - Knowing the correct answer and being able to reason out and explain why it is correct
- Efficiency - Given the numbers, understanding ways to get an answer in a “reasonable amount of time” (Bay-Williams & SanGiovanni, 2021)
- Flexibility - Being able to think about a problem in a variety of ways
- Appropriate Strategy Selection - Being able to look at numbers and reason about which strategies to use based in properties, place value and the relationship between the operations (NCTM, 2000)

## 1.2 Cycle of Engagement

- Concrete - Using concrete materials
- Pictorial - Using pictorial materials
- Abstract - Using symbols and numerals

## 1.3 Automaticity

- Result of fluency
- “Instant popping into of mind” (Logan)
- Getting an answer within three seconds and/or reasonable amount of time without getting bogged down or “stuck.”

## 1.4 Practice

- Students should understand different strategies
- Students should practice using each of those strategies
- Students should practice selecting between the strategies
- Should be meaningful, intentional, purposeful, based on the progression of the operation (Baroody, 2006; Van de Walle, 2007; Henry & Brown, 2008; Boaler, 2015; Bay Williams & SanGiovanni, 2021)

## 1.5 Math Talk

- Students should be explaining their thinking
- Students should be naming their strategies
- Students should have a common language for the strategies they are using across grades
- Students and Teachers should be posing purposeful questions
- Students should be listening to, understanding and critiquing the thinking and reasoning of others (Baroody, 2006; Van de Walle, 2007; Boaler, 2015; Bay Williams & SanGiovanni, 2021)

## 1.6 Modeling Mathematical Thinking

- Represent their thinking with pictures, numbers and words
- Choose and use tools appropriately
- Represent thinking by acting out, using concrete materials, sketches and diagrams (CCSSM, 2010) (NCTM, 2000)

## 1.7 5 Students Engagement

- Students reflect on their work
- Students revise their work
- Students set goals
- Students make action plans for improving
- Teachers encourage and motivate students through positive, informative, feedback
- Teachers promote a growth mindset (Cskikzentmihalyi, 1997; Guskey, 1997; Black & Wiliam, 1998; Dweck, 2006; Marzano, 2007)

# 2

## Shared Definitions

	Beginning	Approaching	Meeting	Exceeding
<p><b>Teachers</b> All teachers have been trained in the elements of the fluency plan. All teachers understand the implementation plan and the teaching components.</p>				
<p><b>Students</b> All students understand the fluency pathway and have a way to self-track and monitor their progress with individual fluency folders.</p>				
<p><b>Parents</b> All parents understand the fluency pathway and have a way to help their students practice at home and monitor their progress. Parent Fluency Workshops should be a part of the implementation plan.</p>				
<b>Notes:</b>				

# 3

## Get the Data - (build fluency profile)

Looking at individual, class, grade, grade band, school trends

	Beginning	Approaching	Meeting	Exceeding
Do you check to see if the students come into the grade at the beginning of the year with at the fluency level from the grade before?				
Do you focus on fluency for 10 minutes a day, collecting evidence of practice sometimes?				
Do you assess fluency at the beginning, middle and end of the year?				
Is fluency more than a unit of study?				
Is fluency practice differentiated for students depending on where they are on the trajectory?				
<b>Notes:</b>				

# 4

## Use the Data

	Beginning	Approaching	Meeting	Exceeding
Make an Individual Fluency Plan				
Student Goal Setting (Do you currently do this?)				
Make Acceleration Plans (Do you currently do this?)				
Map Out Daily Fluency Routines (Do you currently do this?)				
Notes:				

# 5

## Classroom Design

	Beginning	Approaching	Meeting	Exceeding
Differentiated Fluency Workstations (Do you have these?)				
Fluency Anchor Charts (Class) (Do you have all of these?)				
<ul style="list-style-type: none"> <li>• Strategy (What you are doing with numbers)</li> </ul>				
<ul style="list-style-type: none"> <li>• Models (How you are showing your thinking)</li> </ul>				
<ul style="list-style-type: none"> <li>• Learning Target/Success Criteria (What you are teaching and what it looks like when students learn it)</li> </ul>				
Classroom Library (section on fluency books) (Do you have picture books that focus specifically on fluency?)				
Notes:				

# 6

## Materials

	Beginning	Approaching	Meeting	Exceeding
Fact Fluency Folders (Do students have these?)				
Student-created strategy cards (Do you have this?)				
Core set of manipulatives (Do you have these?) <ul style="list-style-type: none"> <li>• domino, dice, 2 sided counters, cubes or snap cubes, highlighter, colored pencils, different types of paper (grid, centimeter, blank), rulers, number paths, beaded number lines, number lines and hundred grids.</li> </ul>				
Notes:				

# 7 Instruction

	Beginning	Approaching	Meeting	Exceeding
Daily Routines- Whole Group (What does this look like?)				
Workstations (How are these structured?)				
• Individual				
• Partner				
• Small Group				
Guided Math Groups (Do you sometimes focus on math fluency?)				
Personalized Goal Setting (Do your students do this?)				
Homework (How do you integrate work on math fact fluency throughout the year?)				
Notes:				

# 8 Assessment (Ongoing)(Which of these do you do?)

	Beginning	Approaching	Meeting	Exceeding
Math Running Records				
Entrance/Exit Slips				
Observations				
Anecdotal				
Interviews				
Conferring				
Student Reflections				
Teacher Made Tests				
Standardized Tests				
Other				
Notes:				

# 9 Analyze the Data What is your plan? (weekly, monthly, quarterly)

	Beginning	Approaching	Meeting	Exceeding
Individually				
Class				
Grade				
Grade Band				
School				
Notes:				

10

# Interpret the Trends and Adjust Instruction Accordingly

(How are you keeping track of this information?)

Beginning

Approaching

Meeting

Exceeding

Individually

Class

Notes: